



LAMARR

INSTITUTE FOR
MACHINE LEARNING
AND ARTIFICIAL
INTELLIGENCE

Splitting Stump Forests: Tree Ensemble Compression for Edge Devices

Fouad Alkhoury and Pascal Welke

Discovery Science 2024 – October 15th

Partner institutions:



Institutionally funded by:



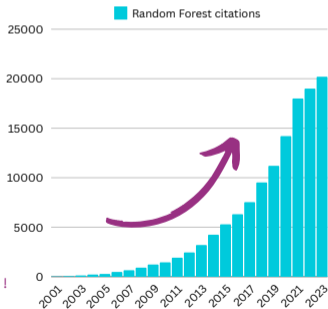
Ministerium für
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138,466
citations

4th
most cited machine
learning paper ever!!



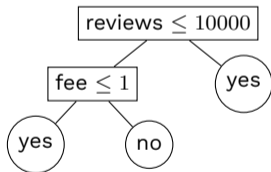
Decision Trees

place	distance	fee	reviews	rating	visit
Pisa Tower	1.3	20	160800	4.7	yes
Cattedrale di Pisa	1.3	8	10923	4.8	yes
Palazzo blu	1.2	5	5205	4.6	no
Tuttomondo	1.8	0	2422	4.6	yes
Botanical Garden	1.0	4	3752	4.4	no
Piazza dei Cavalieri	0.8	0	10534	4.5	yes



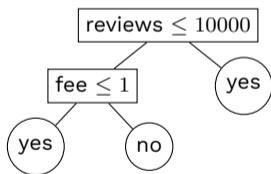
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Decision Trees

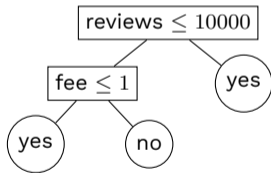
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✓ Interpretable and fast

Decision Trees

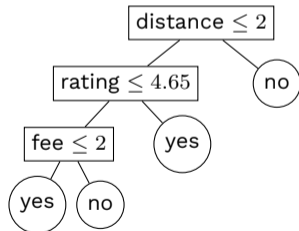
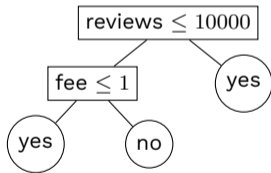
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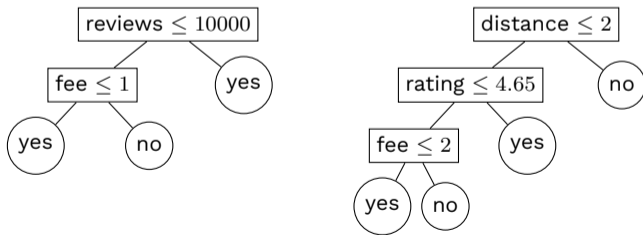
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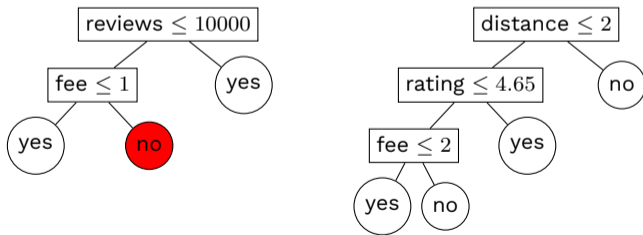
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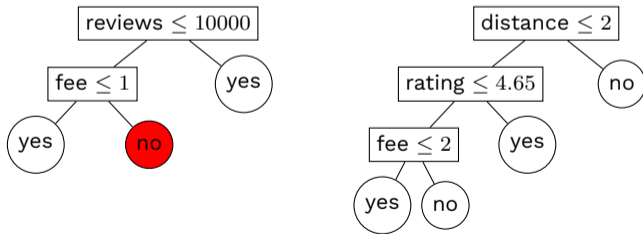
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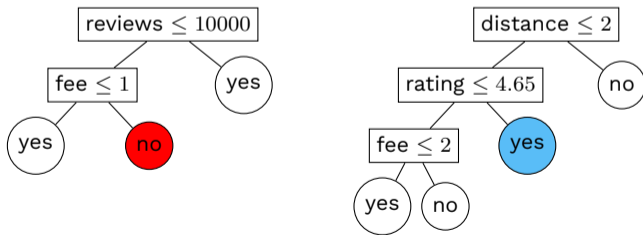
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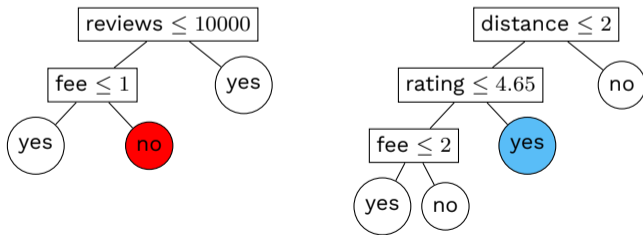
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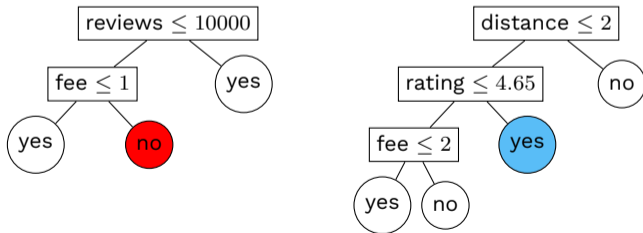


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✗ High variance and sensitivity

Random Forest Tree Ensemble



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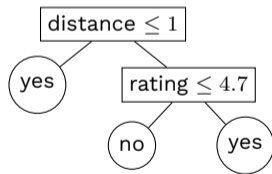


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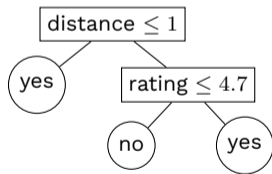
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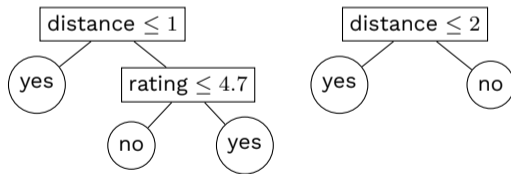
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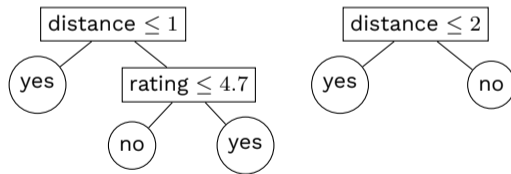
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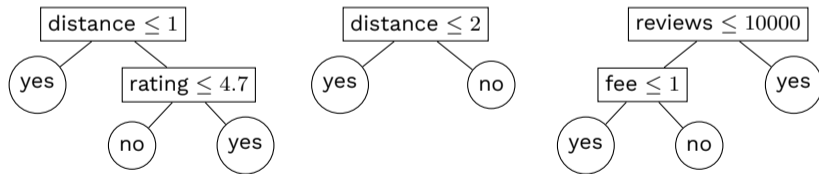
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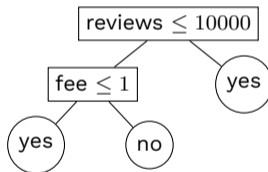
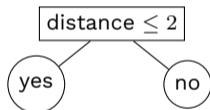
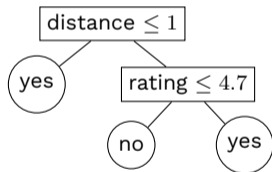
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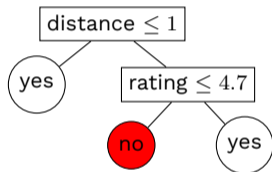


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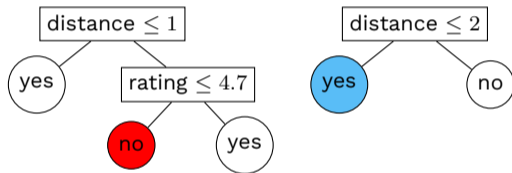
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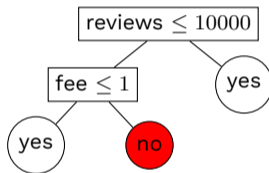
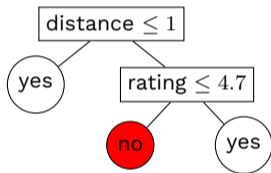
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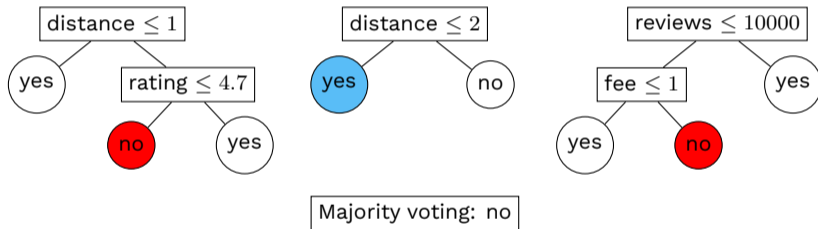
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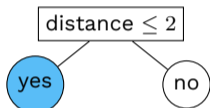
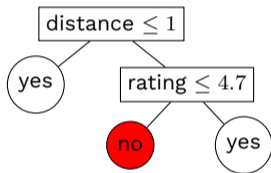
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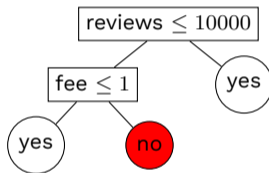
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Majority voting: no

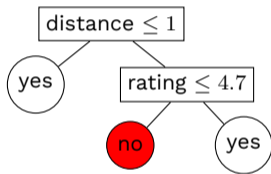


✓ Random forests reduce variance.

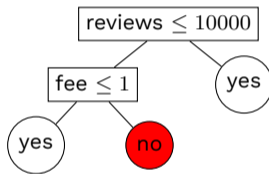
Random Forest Tree Ensemble



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✗ Larger model size

- Real-world datasets are very large (thousands/millions of examples.)



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- Some embedded devices have limited memory.

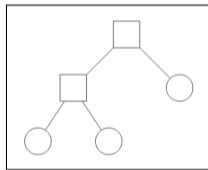


Microcontroller	Flash memory
ATmega169P	16 KB
Arduino Uno	32 KB
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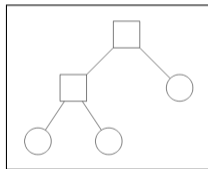


Small random forest

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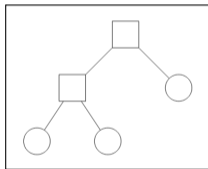
Small random forest

✓ fits within memory

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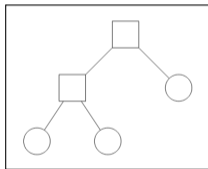
✓ fits within memory

✗ limits the predictive performance

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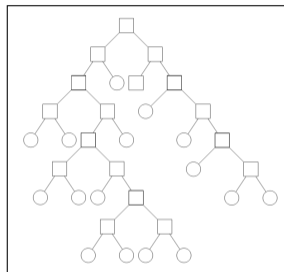
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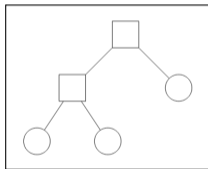


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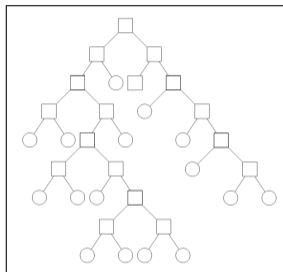
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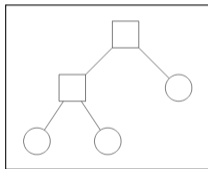
Large random forest

✓ higher predictive performance



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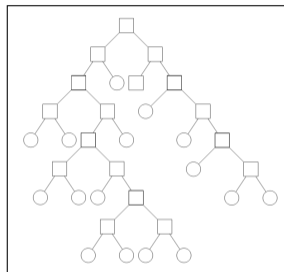
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Small random forest

✓ fits within memory

✗ limits the predictive performance



Large random forest

✓ higher predictive performance

✗ exceeds memory (~ 10 MB)

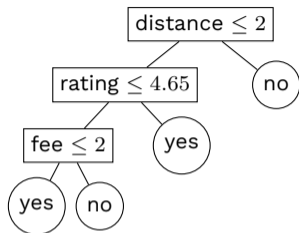
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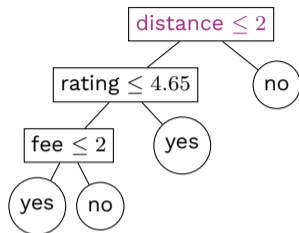
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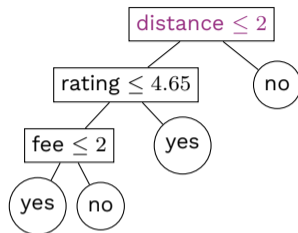
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Tuttomondo	1.8	0	2422	4.6	yes
Botanical Garden	1.0	4	3752	4.4	no
Piazza dei Cavalieri	0.8	0	10534	4.5	yes
Parco Migliarino	5.9	0	10602	4.5	no



- Can we construct a smaller ensemble that preserves the predictive performance?



place	distance	fee	reviews	rating	visit
Pisa Tower	1.3	20	160800	4.7	yes
Cattedrale di Pisa	1.3	8	10923	4.8	yes
Palazzo blu	1.2	5	5205	4.6	no
Tuttomondo	1.8	0	2422	4.6	yes
Botanical Garden	1.0	4	3752	4.4	no
Piazza dei Cavalieri	0.8	0	10534	4.5	yes
Parco Migliarino	5.9	0	10602	4.5	no

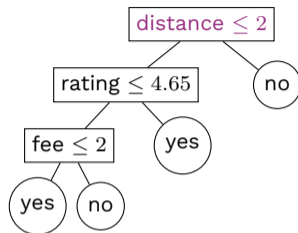


Small subset: good prediction but may cause overfitting.

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place	distance	fee	reviews	rating	visit
Pisa Tower	1.3	20	160800	4.7	yes
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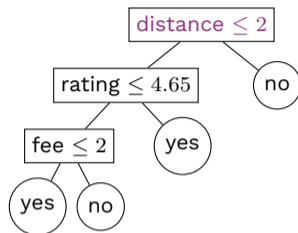
Small subset: good prediction but may cause overfitting.

Large subset: deeper trees, reduced interpretability.

- Can we construct a smaller ensemble that preserves the predictive performance?

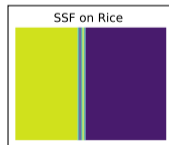
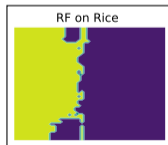
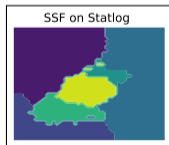
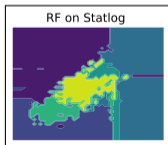


place	distance	fee	reviews	rating	visit
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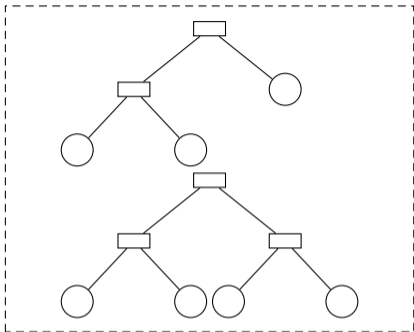
Large subset: deeper trees, reduced interpretability.



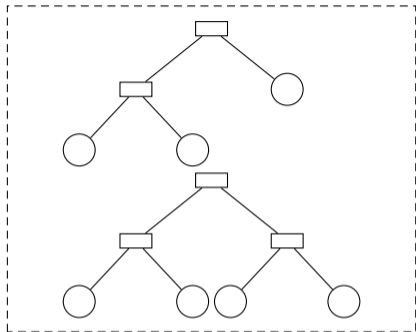


Splitting Stump Forests

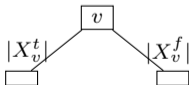
1- Random Forest Training



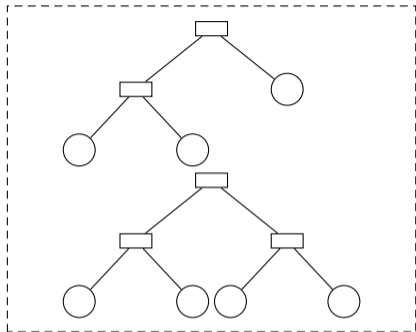
1- Random Forest Training



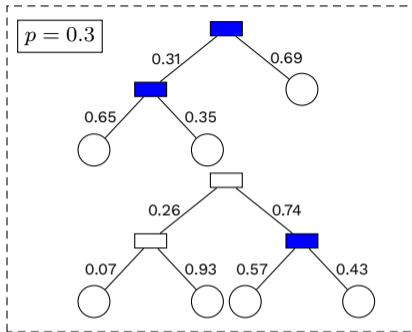
$$\text{score}(v) \leftarrow \frac{\min(|X_v^t|, |X_v^f|)}{|X_v^t| + |X_v^f|}$$



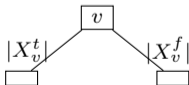
1- Random Forest Training



2- Splitting Node Selection



$$\text{score}(v) \leftarrow \frac{\min(|X_v^t|, |X_v^f|)}{|X_v^t| + |X_v^f|}$$



Balanced splits are selected.

3- Splitting Stump Transformation

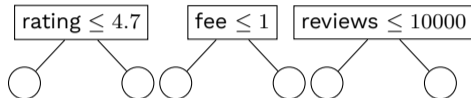


rating \leq 4.7

fee \leq 1

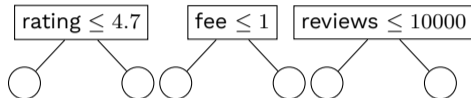
reviews \leq 10000

3- Splitting Stump Transformation



- Transform v into the root of a decision tree T'_v

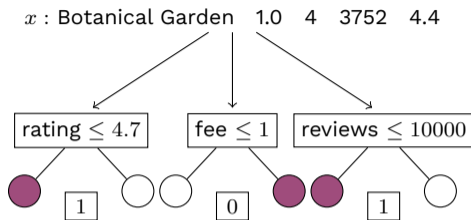
3- Splitting Stump Transformation



- Transform v into the root of a decision tree T'_v
- Define a mapping function $f_{F'} : \mathbb{R}^d \rightarrow \{0, 1\}^k$



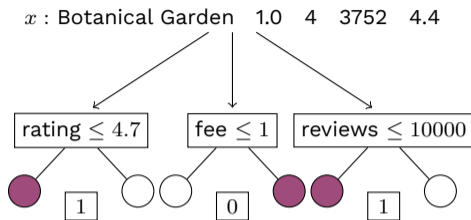
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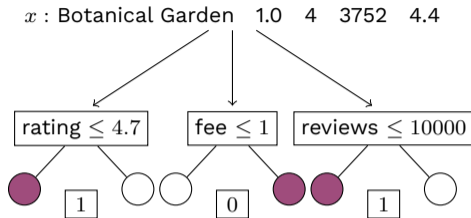
3- Splitting Stump Transformation



- Transform v into the root of a decision tree T'_v
- Define a mapping function $f_{F'} : \mathbb{R}^d \rightarrow \{0, 1\}^k$
- Embed data point x from input vector space into: $\{1, 0, 1\}$ in the SSF space.

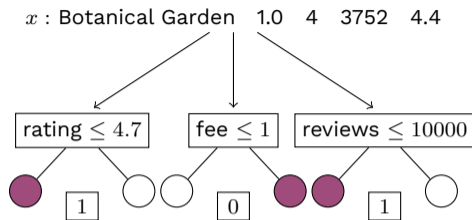
3- Splitting Stump Transformation

4- Training of SSF



- Transform v into the root of a decision tree T'_v
- Define a mapping function $f_{F'} : \mathbb{R}^d \rightarrow \{0, 1\}^k$
- Embed data point x from input vector space into: $\{1, 0, 1\}$ in the SSF space.

3- Splitting Stump Transformation



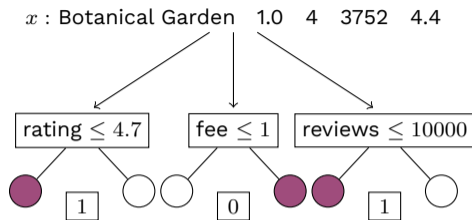
4- Training of SSF

$$(f_{F'}(x), y) = (\{1, 0, 1\}, 0)$$

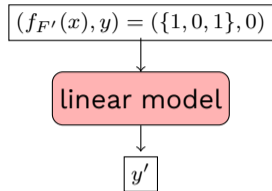
- Transform v into the root of a decision tree T'_v
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3- Splitting Stump Transformation



4- Training of SSF

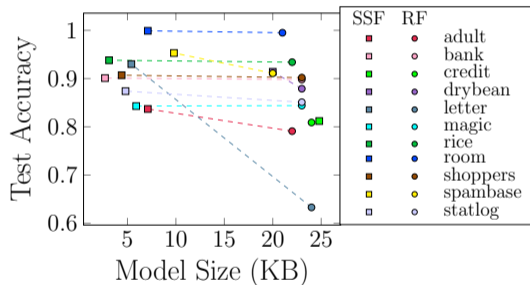


- Transform v into the root of a decision tree T'_v
- Define a mapping function $f_{F'} : \mathbb{R}^d \rightarrow \{0, 1\}^k$
- Embed data point x from input vector space into: $\{1, 0, 1\}$ in the SSF space.
- Apply logistic regression to model the relationship between data representations and target variable



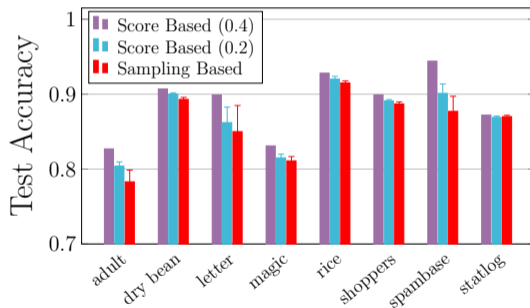
Experiments

- Splitting Stump Forests outperform Random Forest on small embedded devices.



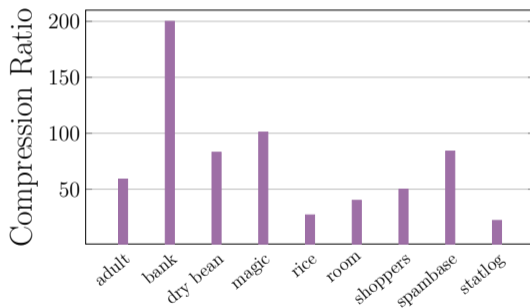
Experiments

- The selected splitting nodes are informative and not accidental.



Experiments

- The compression rate achieved while permitting a 2% accuracy drop.



Experiments



- Splitting Stump Forests outperform competitive methods.

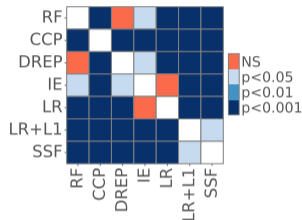
Method		$d = 5$	$d = 10$	$d = 15$	Global
RF (Random Forest)	Acc.	5	4.69	3.23	4.31
	Size	7	7	7	7
	Inf.	6.08	5.46	5.46	5.67
CCP (Cost Complexity Pruning)	Acc.	6.46	6.62	6.85	6.64
	Size	4	2.38	1.85	2.74
	Inf.	4.69	3.54	3.46	3.90
DREP (Diversity Regularized Ensemble Pruning, 2012)	Acc.	4.23	3.62	3.69	3.85
	Size	3.62	4.69	5	4.44
	Inf.	3.07	3.08	2.85	3
IE (Individual Error, 2017)	Acc.	4	3.23	3.38	3.54
	Size	3.69	4.54	5.08	4.43
	Inf.	2.92	3.23	2.92	3.03
LR (Leaf Refinement, 2015)	Acc.	2.69	3.15	4.38	3.41
	Size	5.23	4.77	4.85	4.95
	Inf.	4.92	6.77	6.69	6.13
LR+L1 (Joint Leaf Refinement, 2023)	Acc.	2.23	2.77	2.69	2.56
	Size	3.38	3.46	3	3.28
	Inf.	6	4.85	5.15	5.33
SSF	Acc.	2	2.38	2.39	2.26
	Size	1.23	1.15	1.30	1.23
	Inf.	1.69	1.69	1.92	1.77

Experiments

- Splitting Stump Forests outperform competitive methods.



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Conclusion



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- Splitting Stump Forests extract balanced splitting nodes.

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- Large Random Forest is compressed into a compact model without sacrificing accuracy.

Conclusion



- Splitting Stump Forests extract balanced splitting nodes.
- Large Random Forest is compressed into a compact model without sacrificing accuracy.
- The compressed models are suited for resource-constrained edge devices.



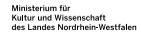
”Like the leaning Tower of Pisa, the Splitting Stump Forests find strength in balance”

Contact: alkhoury@iai.uni-bonn.de

Partner institutions:



Institutionally funded by:





Dataset	16 KB							32 KB						
	RF	CCP	DREP	IE	LR	LRL1	SSF	RF	CCP	DREP	IE	LR	LRL1	SSF
adult	82	81.9	80.5	82.9	84.4	85.7	86.1	85.1	82.3	83.4	84.3	85.9	86.2	86.1
	± 0.4	± 0.3	± 0.2	± 0.6	± 0.4	± 0.3	± 0.3	± 0.3	± 0.4	± 0.4	± 0.5	± 0.3	± 0.3	± 0.3
aloi	96.7	96.2	96.9	96.9	96.1	97.0	97.1	96.8	96.2	96.9	97	96.1	97.1	97.1
	± 0.4	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1	± 0.1
bank	89.9	88.9	89.8	89.7	90.0	90.2	90.1	90	88.9	89.8	89.7	90.1	90.4	90.1
	± 0.1	± 0.5	± 0.1	± 0.1	± 0.3	± 0.3	± 0.2	± 0.1	± 0.3	± 0.1	± 0.1	± 0.2	± 0.2	± 0.1
credit	81	80.7	80.8	81.1	81.4	81.1	81.1	80.9	80.7	81	81.3	81.4	80.9	81.2
	± 0.2	± 0.3	± 0.1	± 0.2	± 0.3	± 0.1	± 0.2	± 0.1	± 0.2	± 0.1	± 0.1	± 0.2	± 0.1	± 0.1
dry bean	88.1	85.4	89.1	88.7	89.2	91.8	91.4	87.9	87.4	89.3	89.9	89.4	91.8	91.4
	± 0.7	± 0.3	± 0.1	± 0.3	± 0.3	± 0.1	± 0.4	± 1.0	± 0.4	± 0.5	± 0.6	± 0.5	± 0.3	± 0.4
letter	62.5	64.3	62.6	62.1	62.9	76.3	93.0	63.3	61.2	65.9	65.8	78.2	71.4	93.0
	± 2.2	± 1.1	± 0.9	± 1.2	± 0.9	± 0.9	± 1.7	± 3.6	± 1.4	± 1.0	± 1.7	± 1.5	± 1.4	± 1.9
magic	84.9	83.2	83.7	84.2	84.9	85.8	86.3	86	83.5	83.8	83.9	86.1	86.5	86.3
	± 0.5	± 0.9	± 0.5	± 0.5	± 0.01	± 0.2	± 0.7	± 0.7	± 0.7	± 0.3	± 0.5	± 0.6	± 0.2	± 0.4
rice	92.5	93.7	93.1	0.93	93.2	93.5	93.8	93.4	93.7	93.6	93.5	93.2	93.5	93.8
	± 0.6	± 0.7	± 0.3	± 0.4	± 0.7	± 0.1	± 0.1	± 0.7	± 0.5	± 0.2	± 0.3	± 0.6	± 0.1	± 0.1
room	99.2	97.0	99.5	99.6	99.2	99.8	99.9	99.5	99.3	99.7	99.9	99.2	99.8	99.9
	± 0.3	± 0.4	± 0.1	± 0.2	± 0.6	± 0.2	± 0.2	± 0.1	± 0.2	± 0.1	± 0.2	± 0.3	± 0.1	± 0.1
shoppers	87.2	86.9	90.1	91.0	91.6	91.3	90.7	90.2	86.9	90.3	91.2	91.6	91.3	90.7
	± 1.5	± 0.6	± 0.3	± 0.2	± 0.4	± 0.3	± 0.4	± 1.2	± 0.2	± 0.4	± 0.1	± 0.4	± 0.2	± 0.2
spambase	90.8	91.3	90.9	92.4	91.6	92.7	95.3	91.1	91.7	92.9	92.4	94.3	93.2	95.3
	± 0.6	± 0.4	± 0.2	± 1.0	± 0.5	± 0.2	± 0.4	± 0.6	± 0.6	± 0.6	± 1.2	± 0.4	± 0.2	± 0.2
statlog	85.2	84.1	84.7	84.8	84.9	86.5	87.4	85.1	84.9	84.8	84.7	87.1	87.9	87.4
	± 1.6	± 1.0	± 0.4	± 0.4	± 0.8	± 0.2	± 0.3	± 0.8	± 0.6	± 0.7	± 0.6	± 0.5	± 0.2	± 0.1
waveform	96.9	95.1	96.9	96.9	96.9	97.0	97.1	96.6	95.1	97	97	96.9	97.2	97.1
	± 0.2	± 0.2	± 0.1	± 0.1	± 0.3	± 0.1	± 0.1	± 0.2	± 0.1	± 0.1	± 0.1	± 0.2	± 0.1	± 0.1
avg rank	4.79	5.86	4.79	4.17	3.94	2.09	1.54	4.72	6.32	4.45	4.28	3.51	2.1	1.88