

Three-Hop Distance Estimation in Social Graphs

Pascal Welke, Alexander Markowetz, Torsten Suel, Maria Christoforaki

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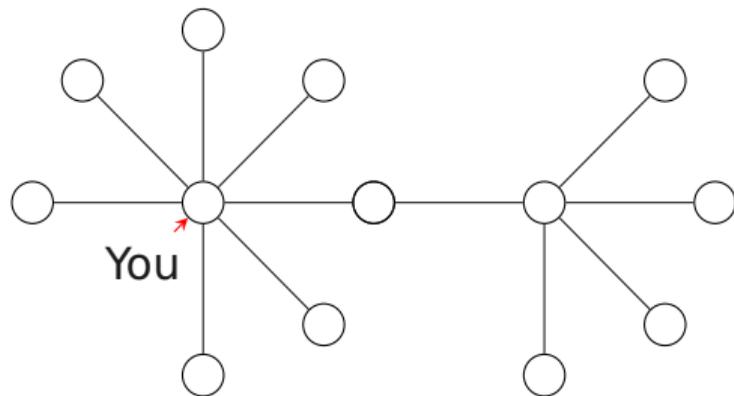
Social Search

Three-Hop Distance Estimation in Social Graphs

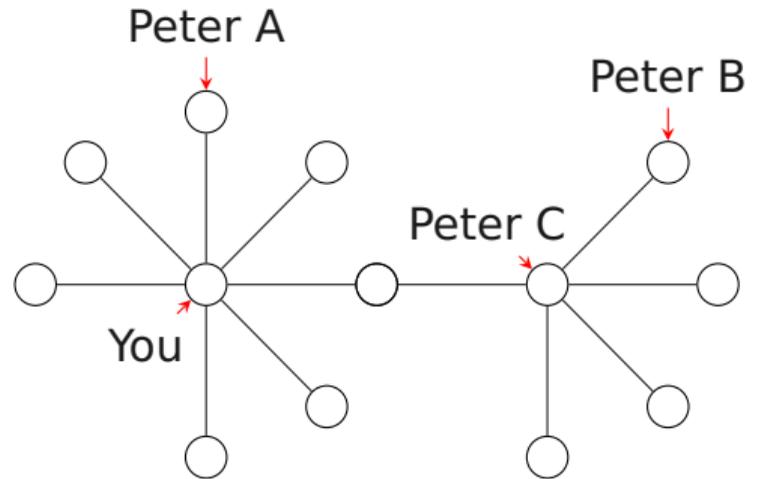
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Three-Hop Distance Estimation in Social Graphs



Social Search

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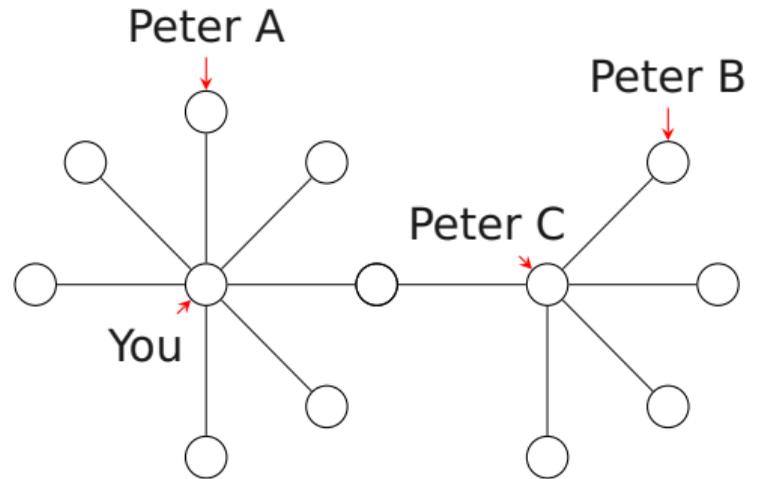
Social Search

Three-Hop Distance Estimation in Social Graphs

 →

Results

- Peter A
- Peter C
- Peter B



Distance Estimation for Social Search

Three-Hop Distance Estimation in Social Graphs

- Social graphs may have millions of vertices and billions of edges
 - Running a shortest path algorithm for each query at runtime is infeasible (runtime constraints)
 - Computing and storing all distances in advance is infeasible (space constraints)

Distance Estimation for Social Search

Three-Hop Distance Estimation in Social Graphs

- Social graphs may have millions of vertices and billions of edges
 - Running a shortest path algorithm for each query at runtime is infeasible (runtime constraints)
 - Computing and storing all distances in advance is infeasible (space constraints)
- Distance signals are one factor among many others in social search
 - Exact distances are not always required

Distance Estimation for Social Search

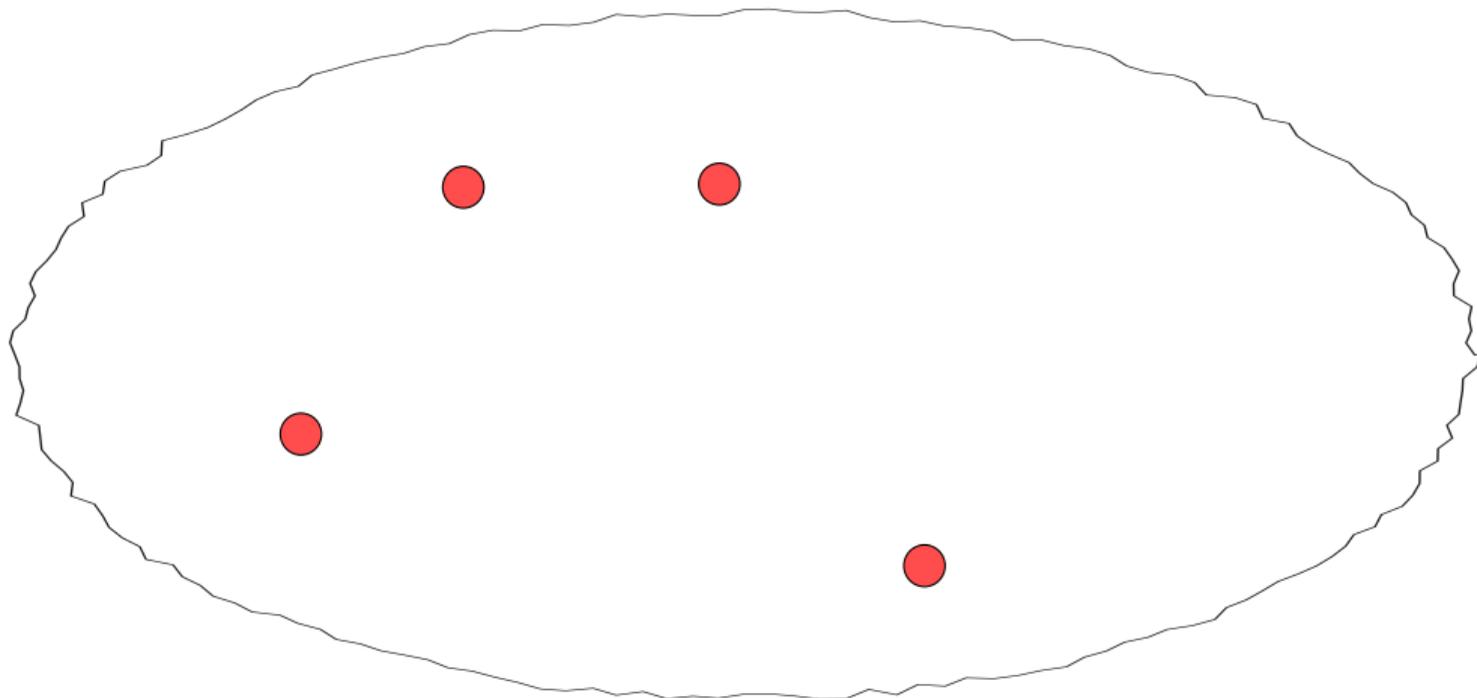
Three-Hop Distance Estimation in Social Graphs

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- Distance signals are one factor among many others in social search
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Problem: For a graph $G = (V, E)$, compute a data structure of size $O(|V| + |E|)$ that allows fast approximate answers to distance queries for arbitrary pairs of vertices $s, t \in V$.

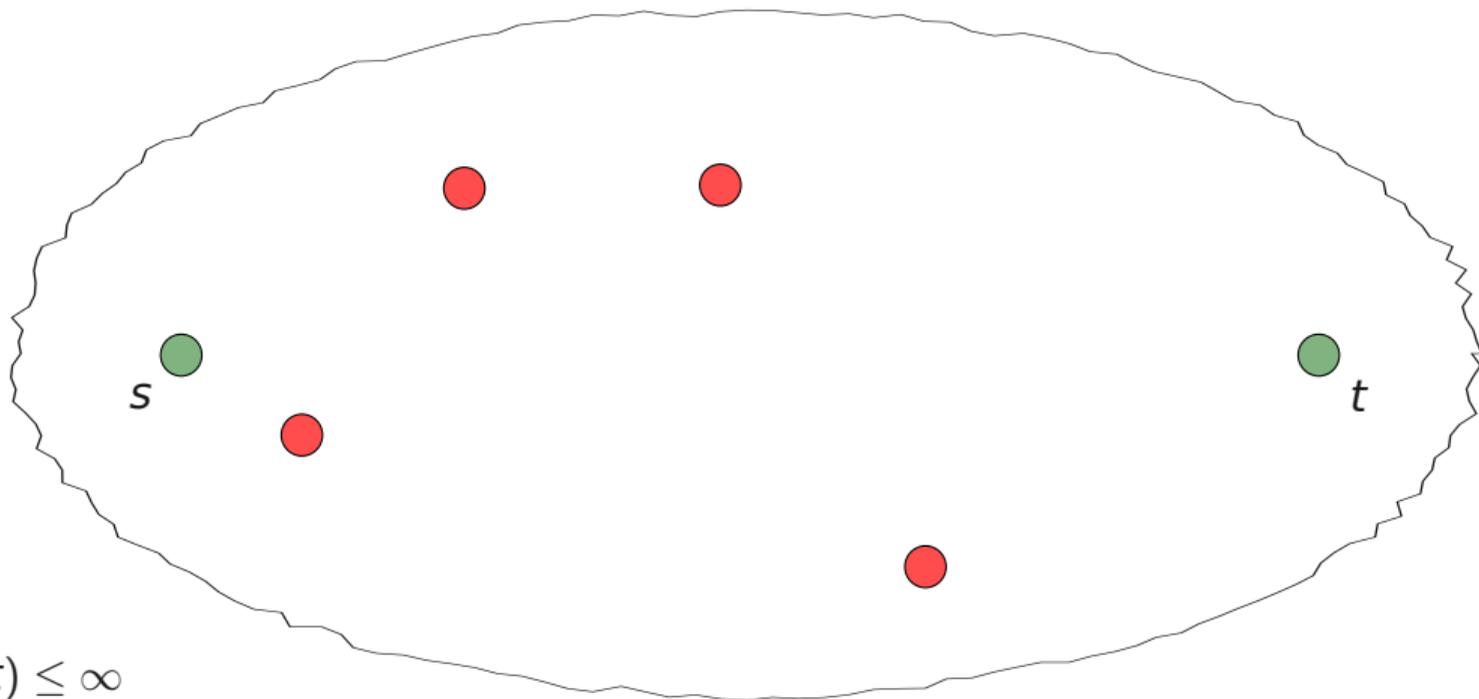
Classical Approach: Two-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs



Classical Approach: Two-Hop Landmarks

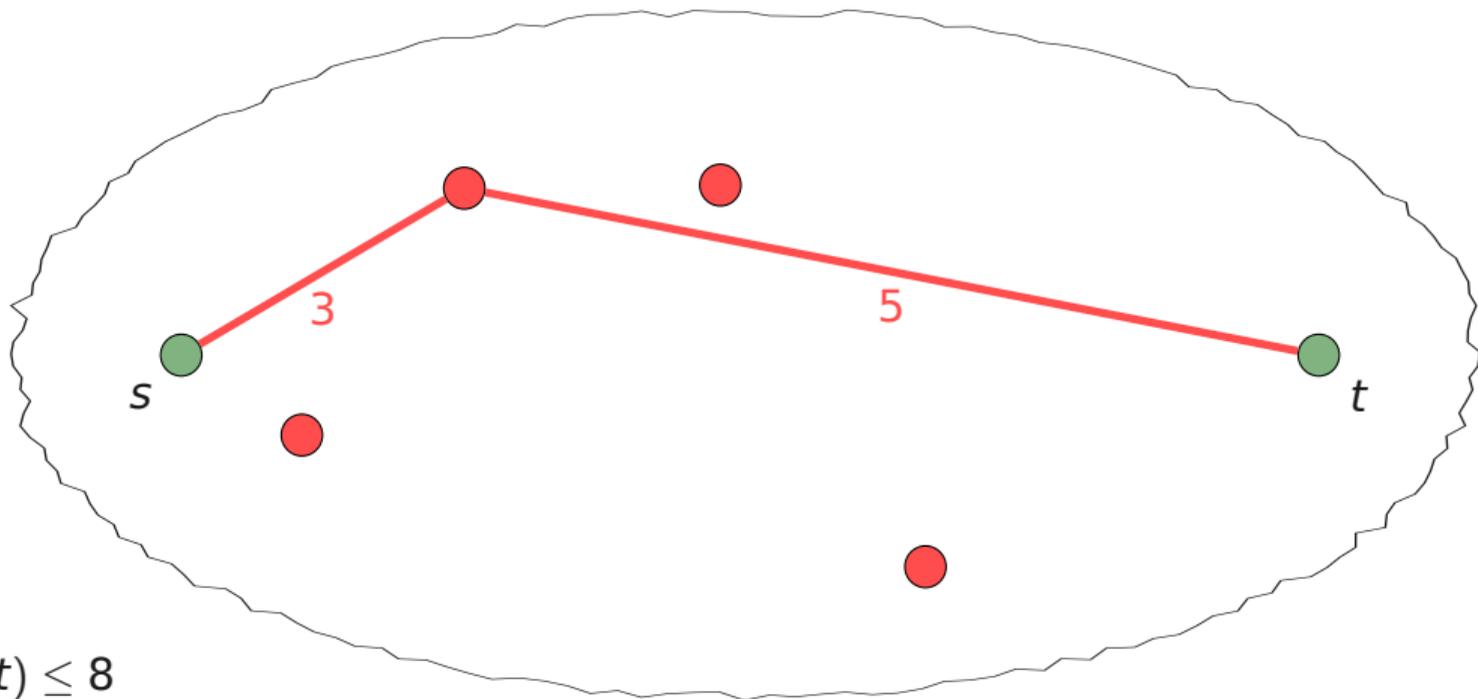
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq \infty$$

Classical Approach: Two-Hop Landmarks

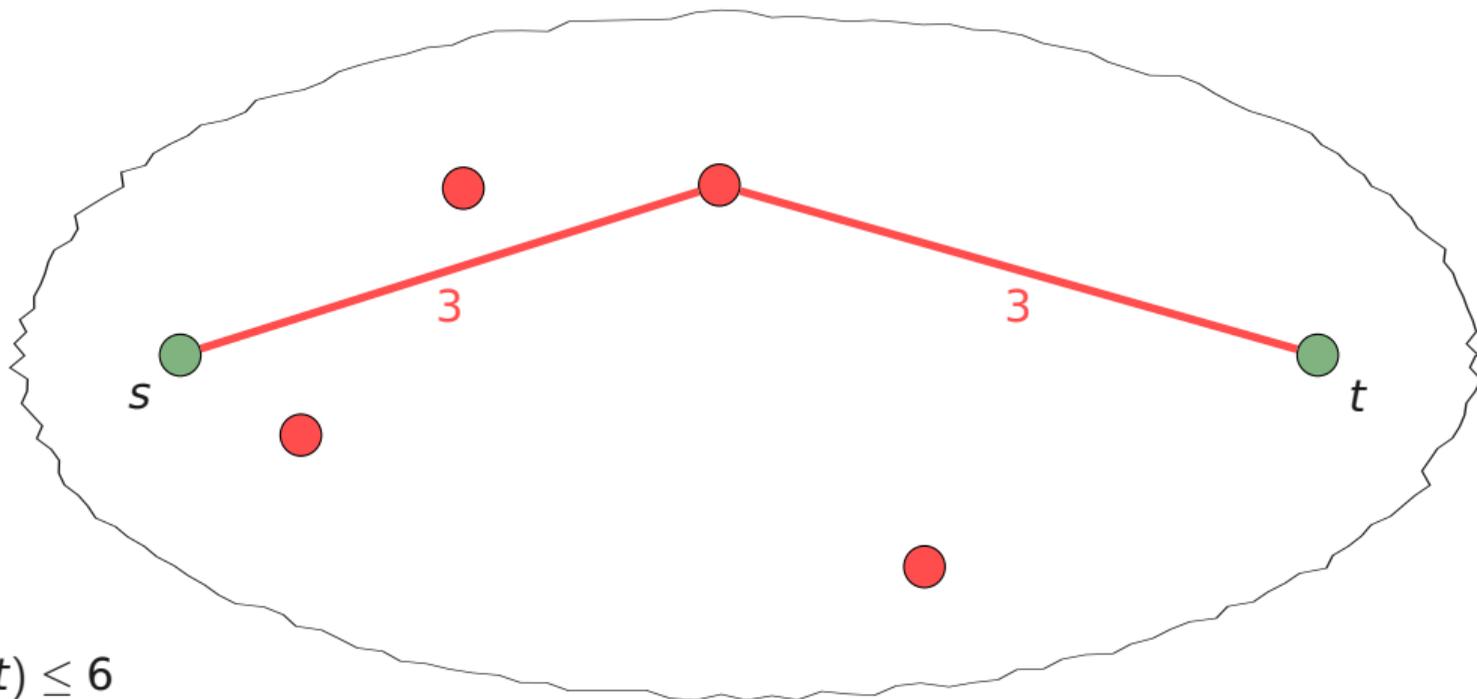
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 8$$

Classical Approach: Two-Hop Landmarks

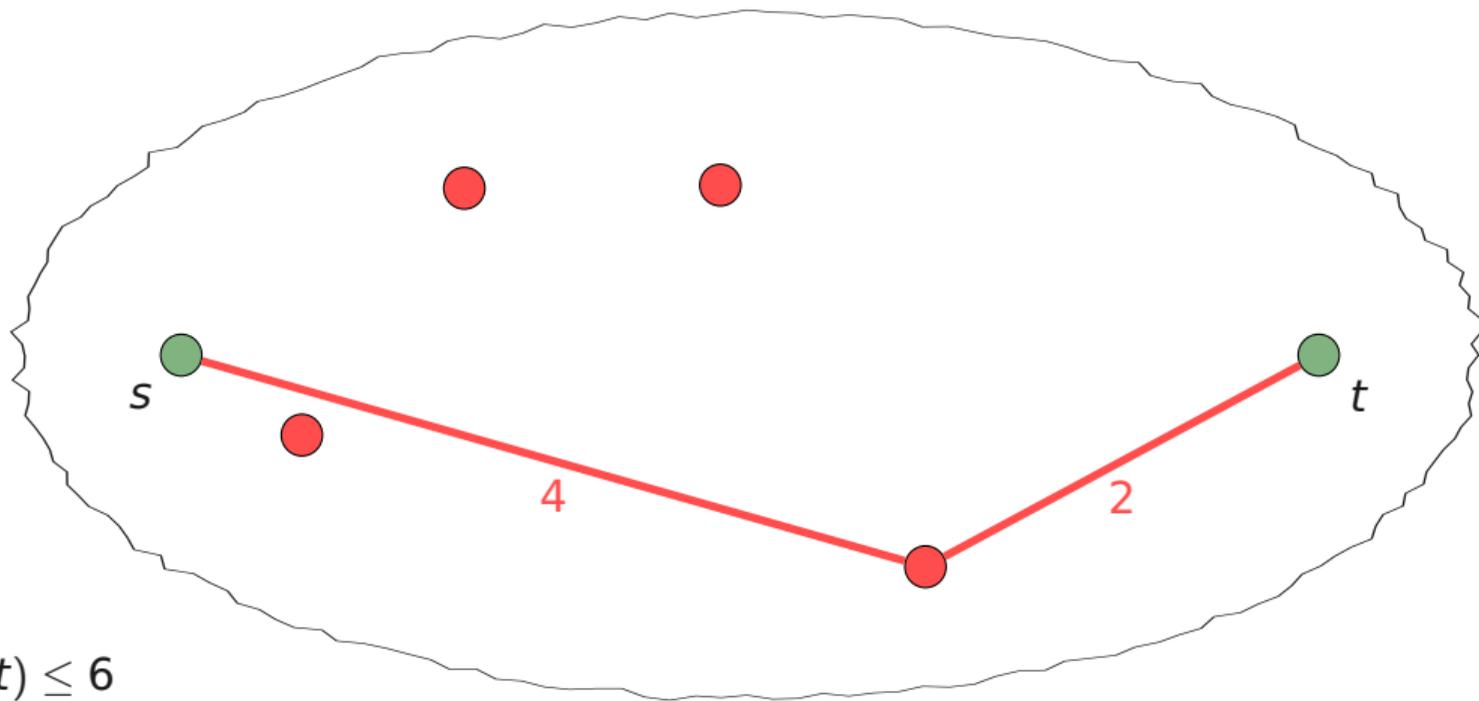
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 6$$

Classical Approach: Two-Hop Landmarks

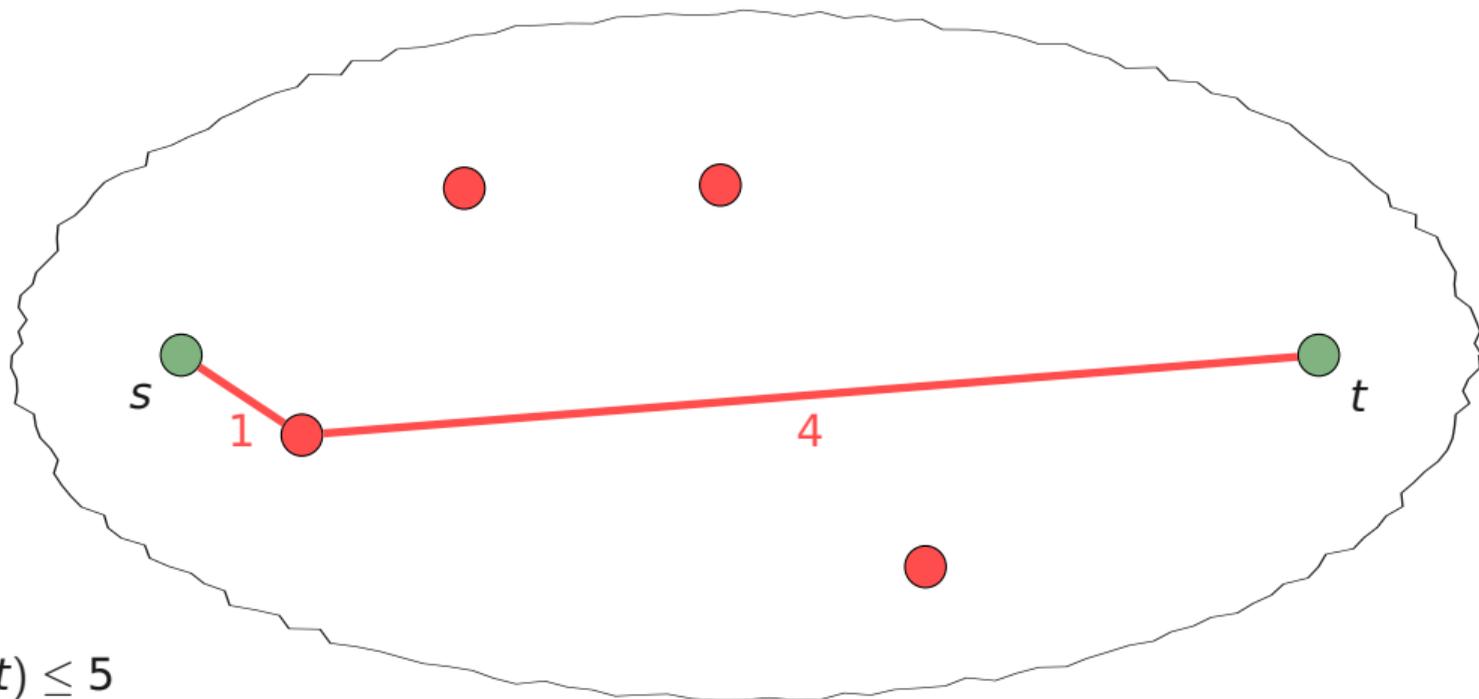
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 6$$

Classical Approach: Two-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 5$$

Problems with Two-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs

- We have to store distances from all landmarks to all vertices

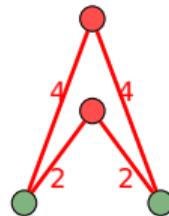
	l_1	l_2	\dots	$l_{ L }$
v_1				
v_2				
\vdots				
v_n				

Problems with Two-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs

- We have to store distances from all landmarks to all vertices
- We need landmarks close to shortest paths for any given query

	l_1	l_2	\dots	$l_{ L }$
v_1				
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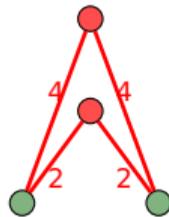


Problems with Two-Hop Landmarks

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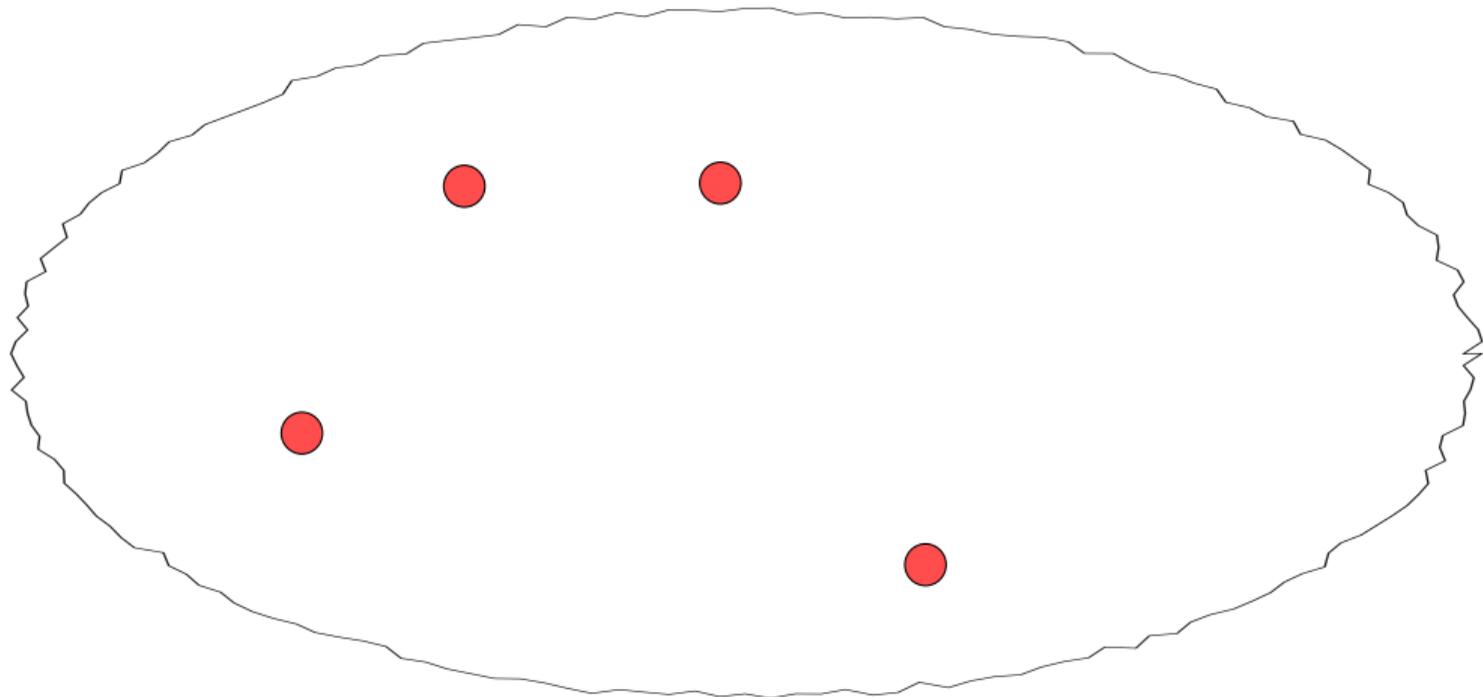
- We have to store distances from all landmarks to all vertices
- We need landmarks close to shortest paths for any given query
- The stored data needs to grow superlinearly for good results

	l_1	l_2	\dots	$l_{ L }$
v_1				
v_2				
\vdots				
v_n				



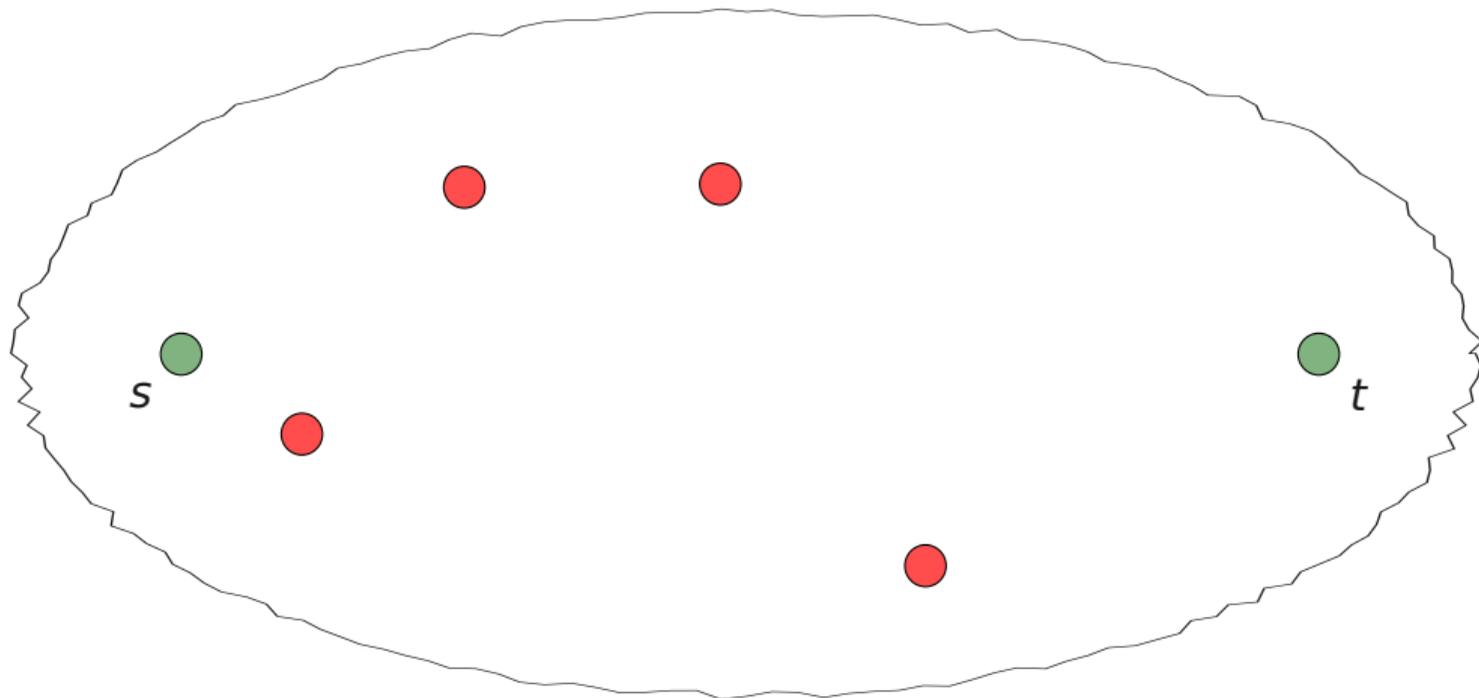
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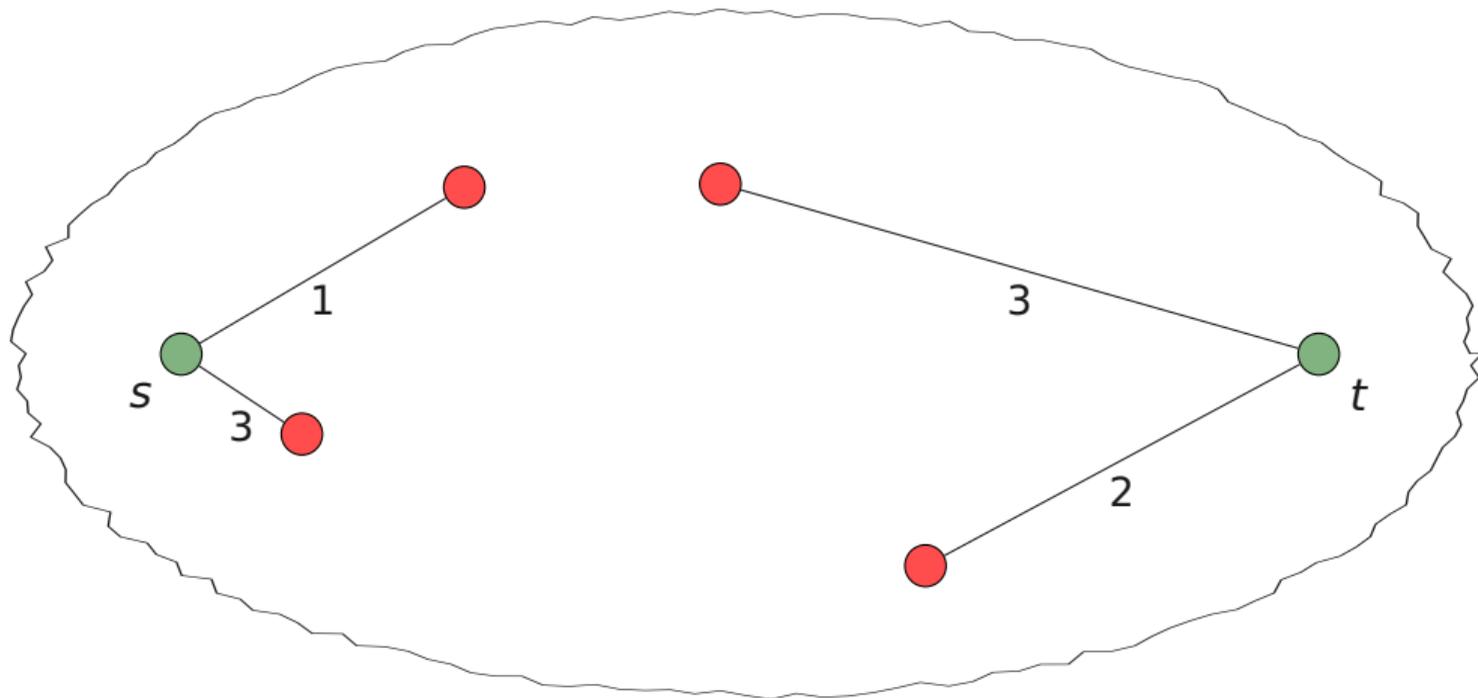
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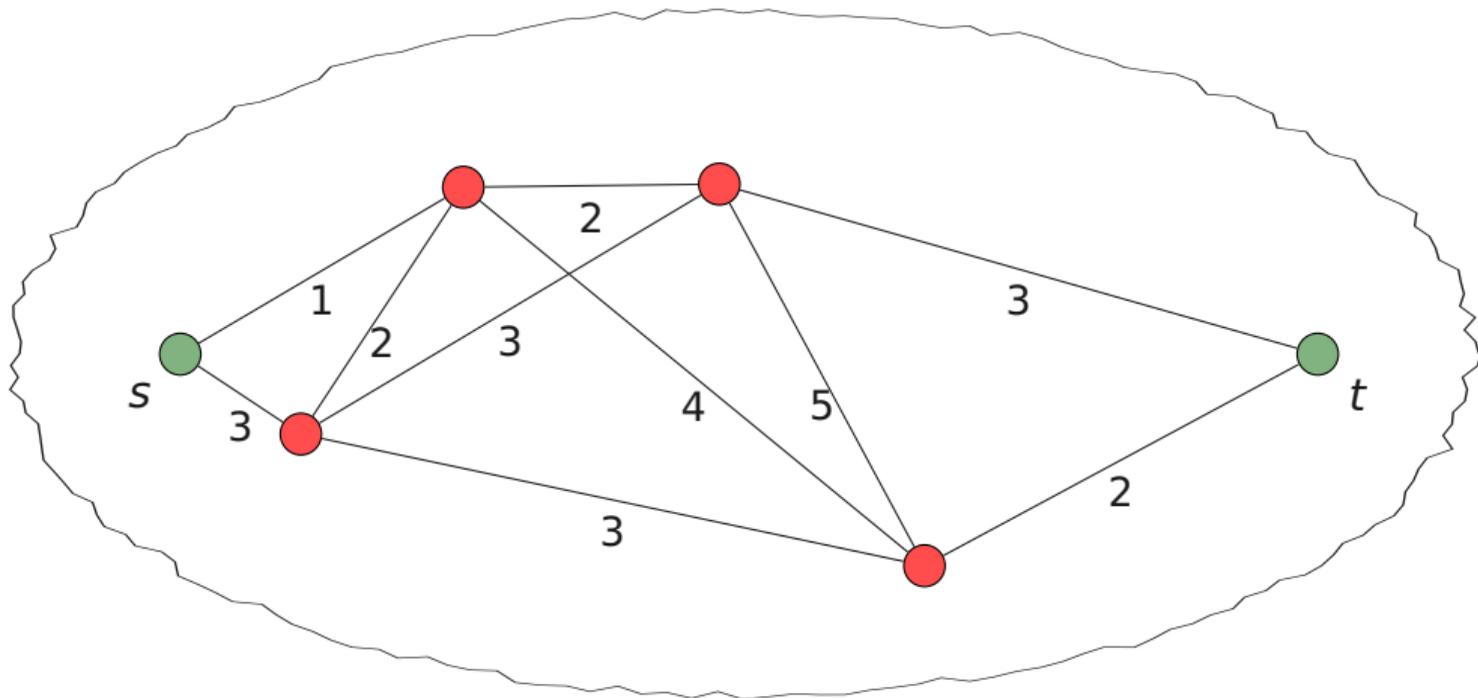
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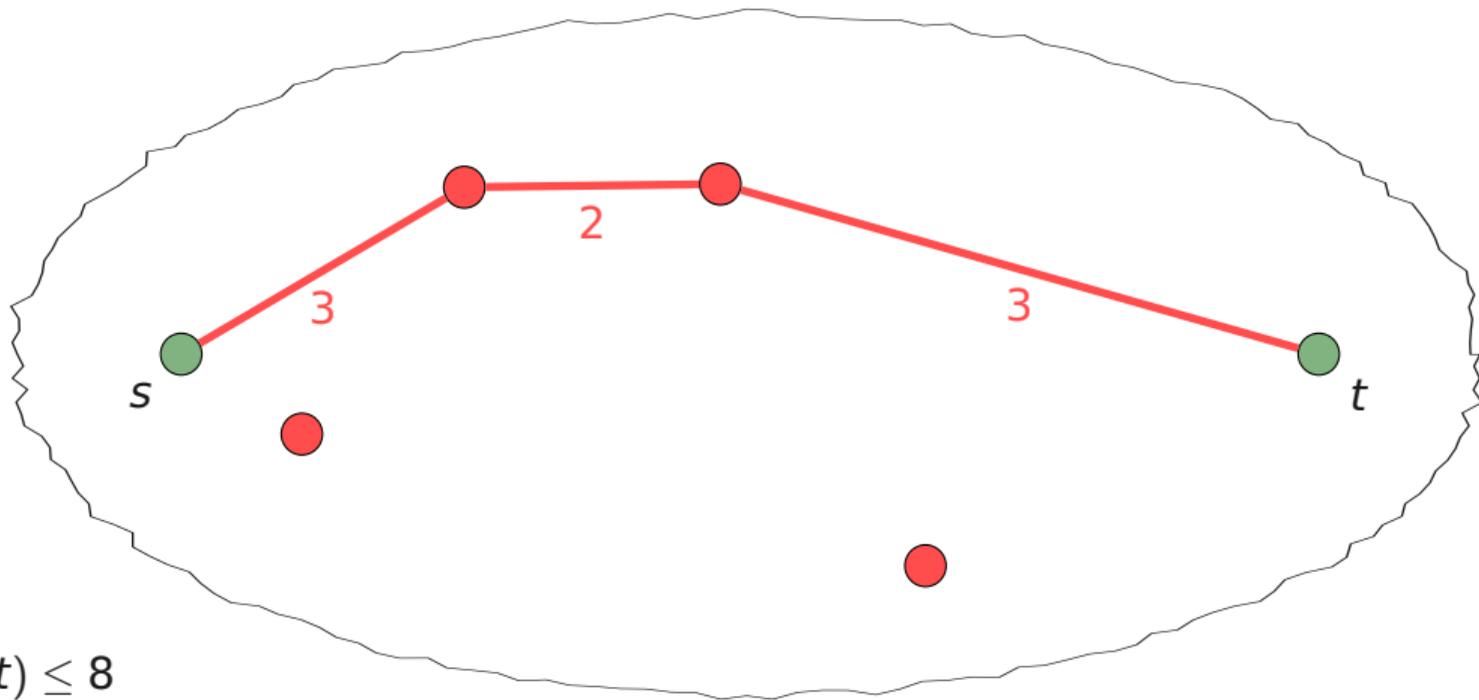
Three-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs



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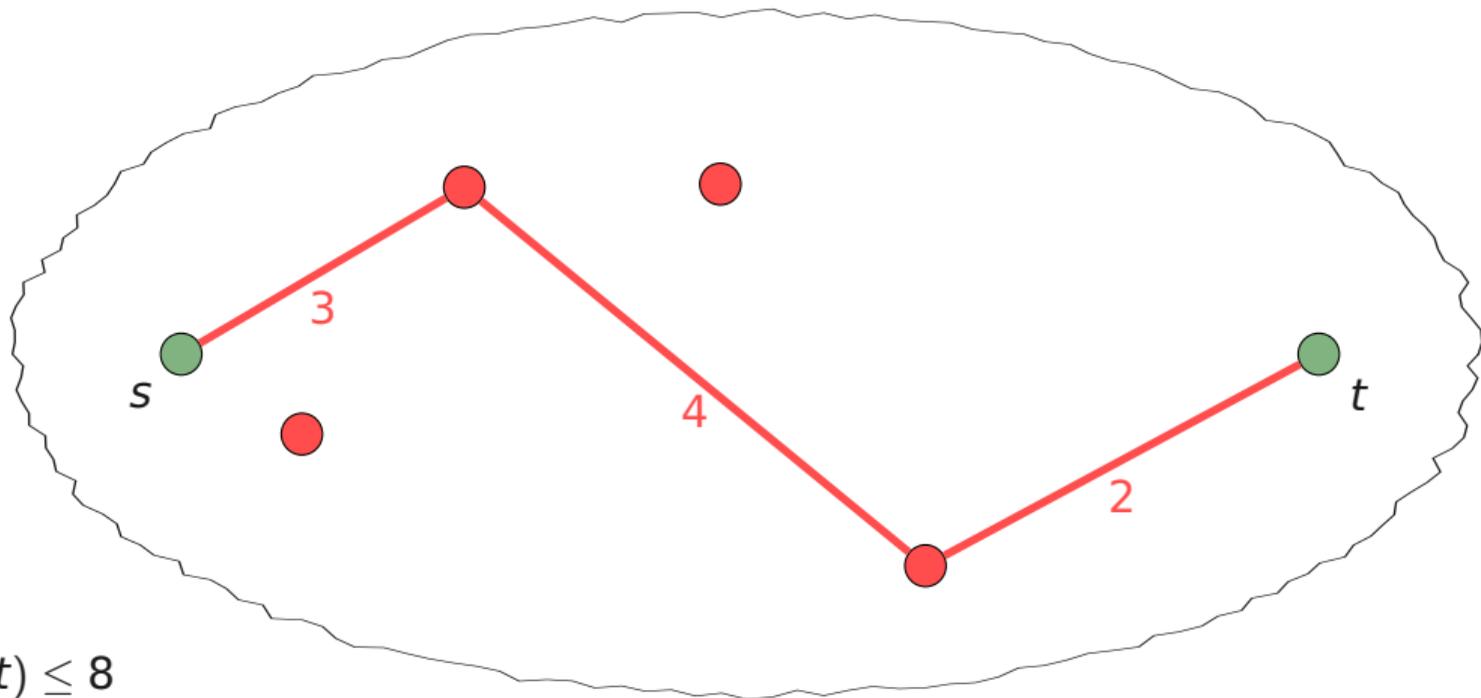
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 8$$

Three-Hop Landmarks

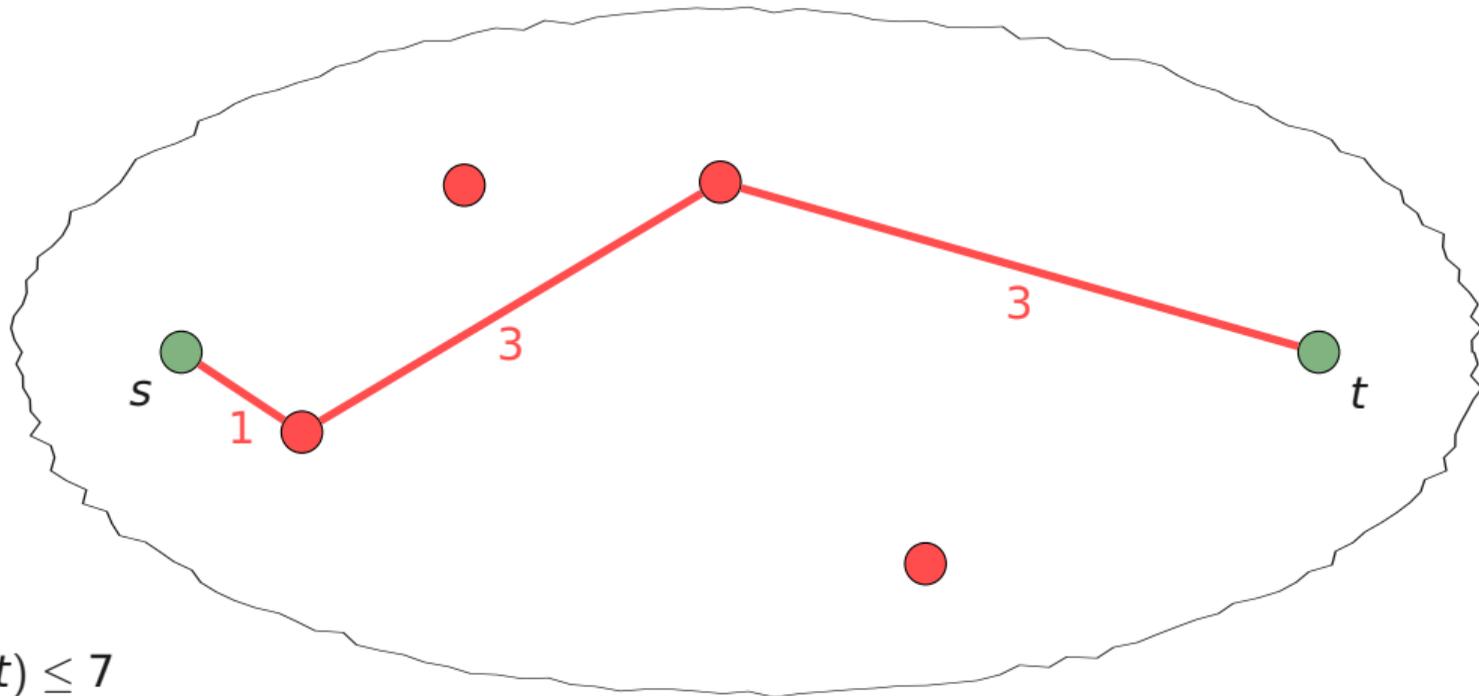
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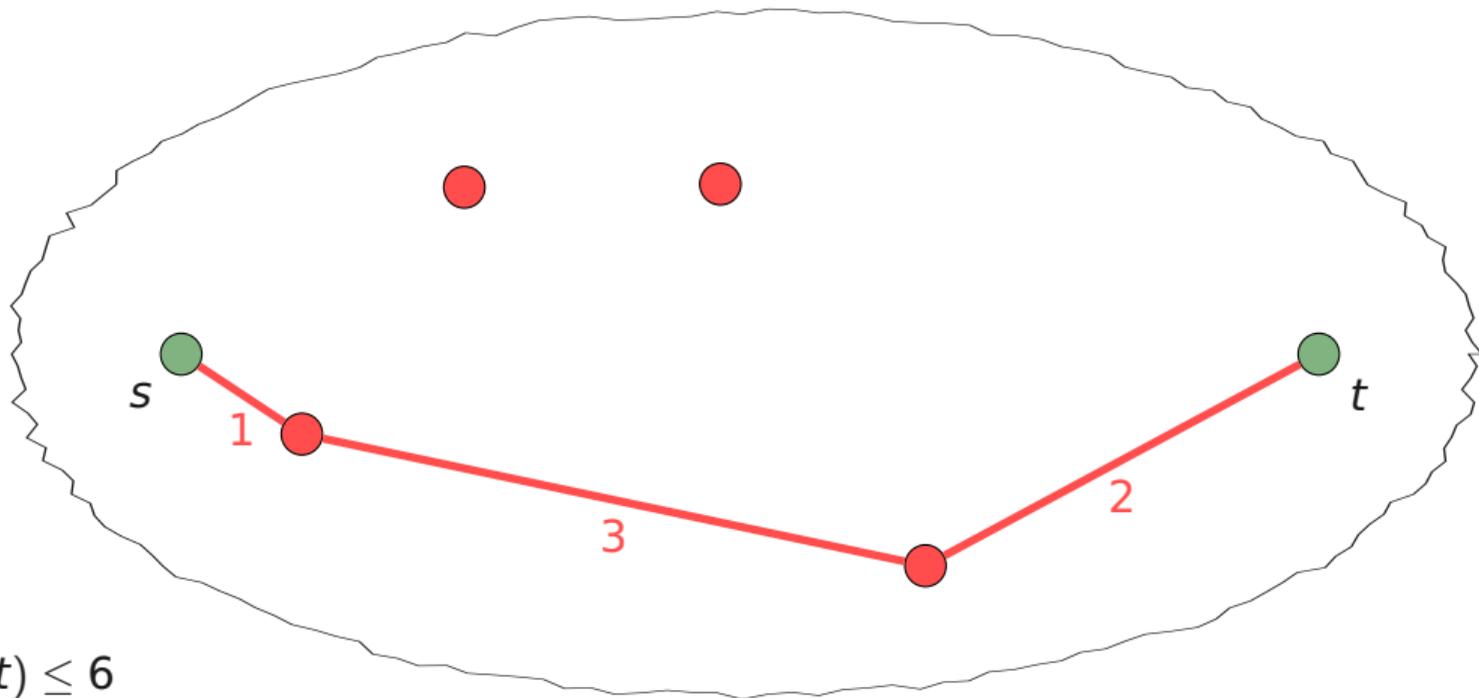
Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 7$$

Three-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs



$$d(s, t) \leq 6$$

Benefits & Drawbacks of Three-Hop Landmarks

Three-Hop Distance Estimation in Social Graphs

Pros:

- Close landmarks have a higher likelihood to be close to shortest paths
- We can have up to $\sqrt{|V|}$ landmarks in a $O(|V|)$ space data structure
- A small number of local landmarks suffices

Cons:

- Going over two landmarks gives less tight bounds
- Algorithms and data structures get more complicated

Which Approach is Better?

Three-Hop Distance Estimation in Social Graphs

Two-Hop

	l_1	l_2	\dots	$l_{ L }$
v_1				
v_2				
\vdots				
v_n				

Three-Hop

	l_1	l_2	\dots	$l_{ L }$
v_1				
v_2				
\vdots				
v_n				

$v_1 \rightarrow [(l_{1_1}, 1), \dots, (l_{1_k}, 2)]$
 $v_2 \rightarrow [(l_{2_1}, 1), \dots, (l_{2_k}, 2)]$
 \vdots
 $v_n \rightarrow [(l_{n_1}, 1), \dots, (l_{n_k}, 2)]$

Which Approach is Better?

Three-Hop Distance Estimation in Social Graphs

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Three-Hop

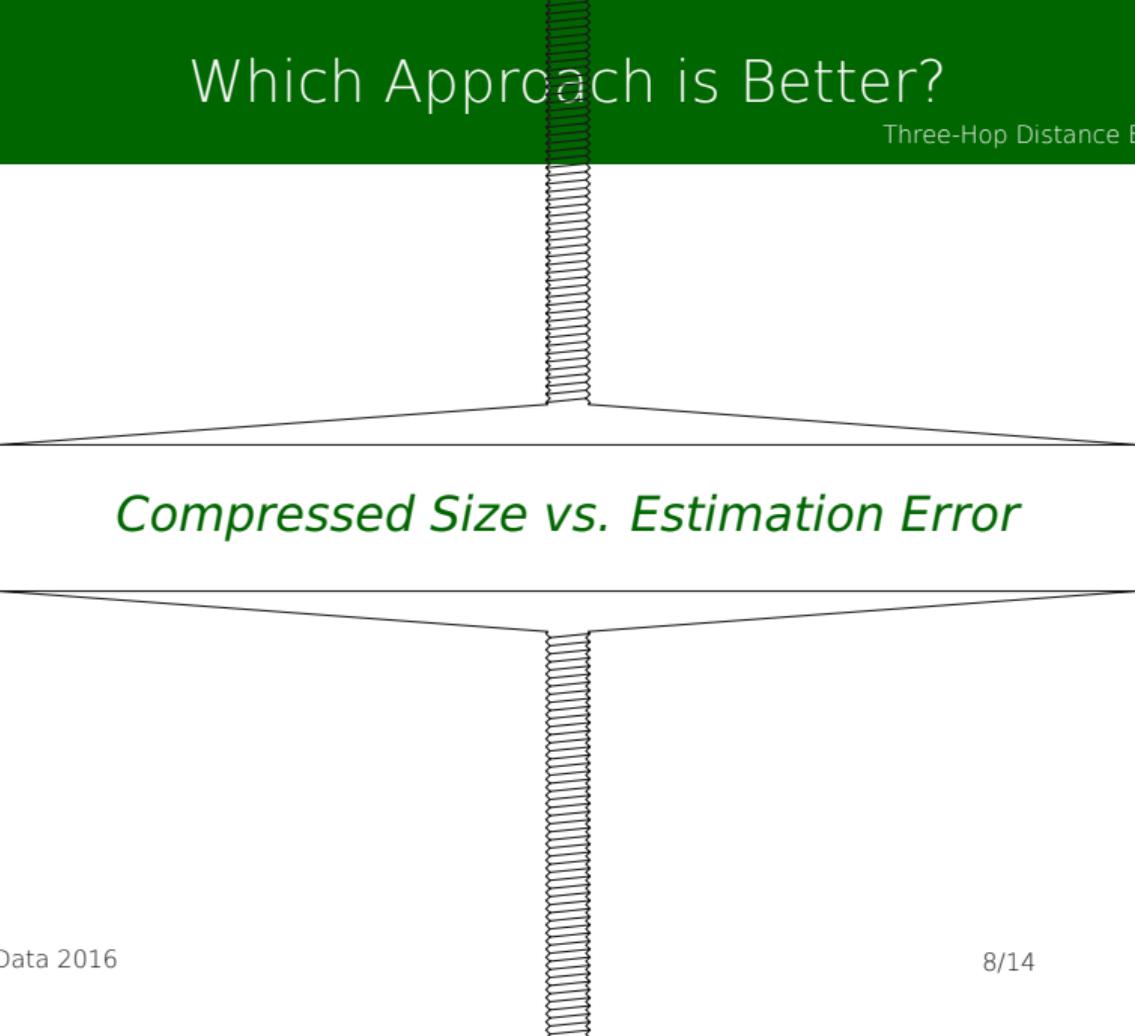
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Which Approach is Better?

Three-Hop Distance Estimation in Social Graphs



Compressed Size vs. Estimation Error

Compressing Two-Hop Landmark Data

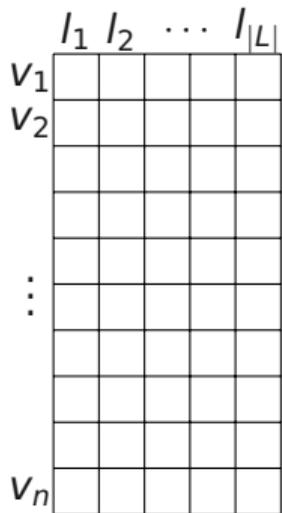
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Compressing Two-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

Single Row Compression

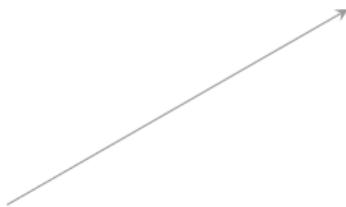


Compressing Two-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

Single Row Compression

	l_1	l_2	\dots	$l_{ L }$
v_1				
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v_n				



v:

3	2	1	4	3
---	---	---	---	---

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Single Row Compression

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- Distances are small

- Use Rice coding

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Neighbor List Compression

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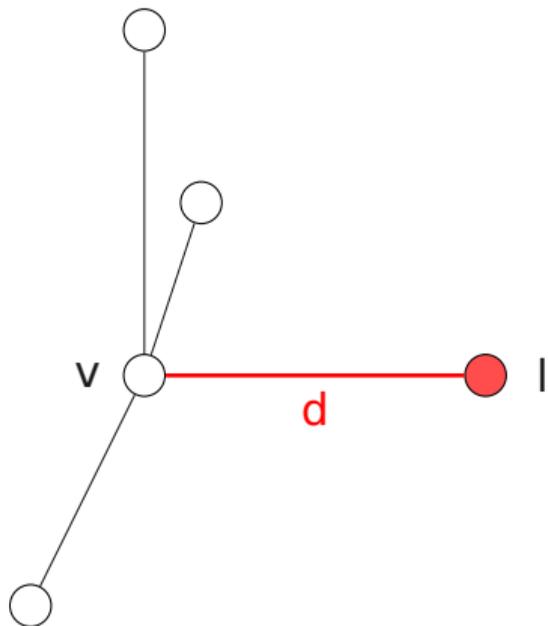
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Three-Hop Distance Estimation in Social Graphs



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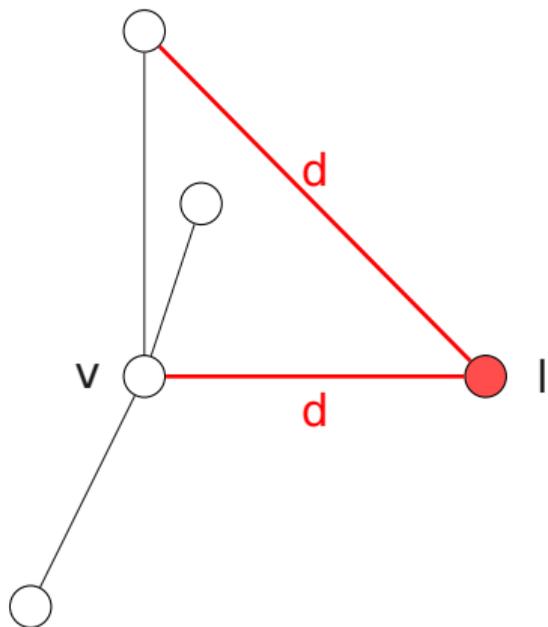
- Neighbors are very similar

v:

3	2	1	4	3
---	---	---	---	---

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Three-Hop Distance Estimation in Social Graphs



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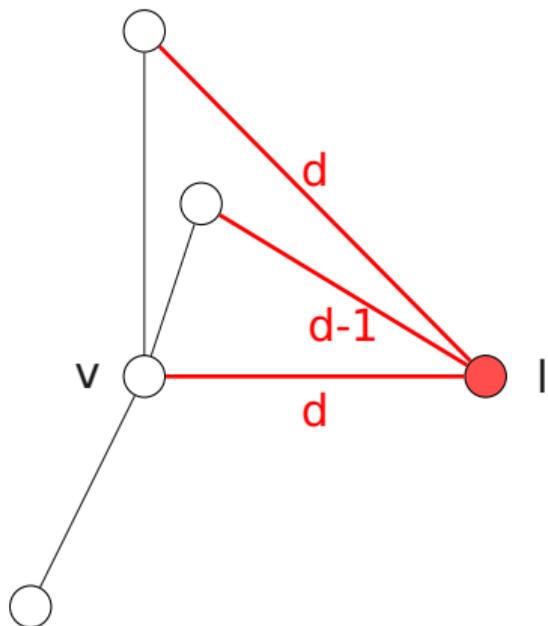
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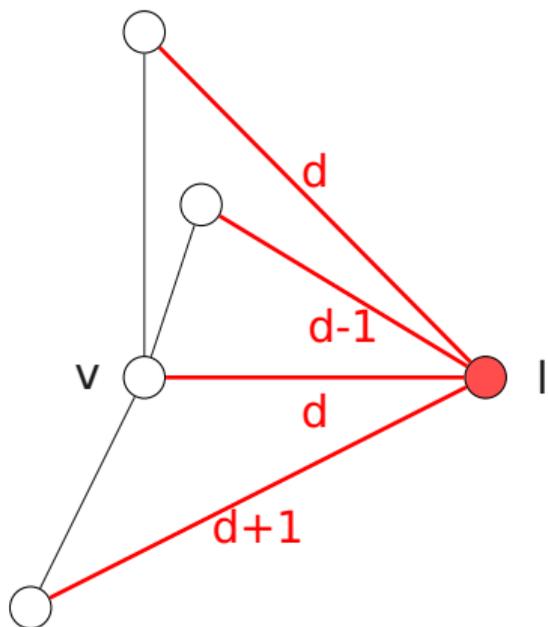
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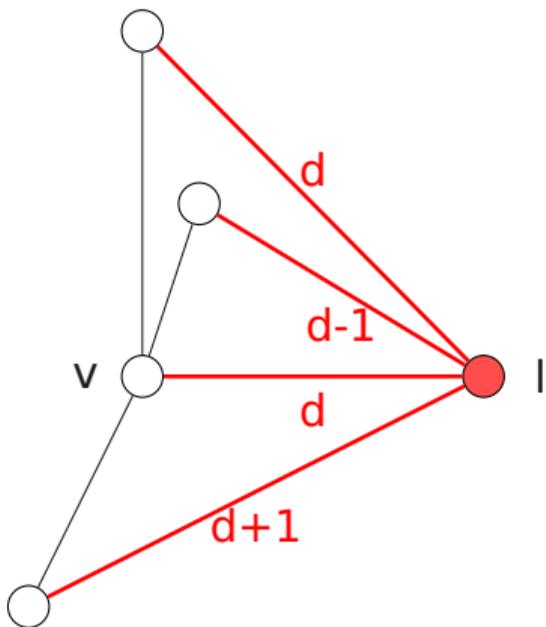
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Compressing Two-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs



Single Row Compression

v:

3	2	1	4	3
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Neighbor List Compression

w:

3	3	2	3	3
---	---	---	---	---

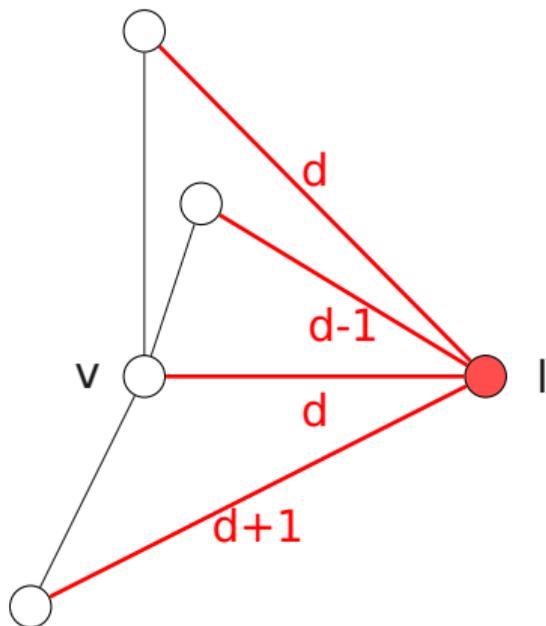
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Compressing Two-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs



Single Row Compression

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---	---	---	---	---

- Distances are small

- Use Rice coding

Neighbor List Compression

w:

3	3	2	3	3
---	---	---	---	---

- Neighbors are very similar

v:

3	2	1	4	3
---	---	---	---	---

- Use relative encoding

0	-1	-1	1	0
---	----	----	---	---

- less than two bits/distance

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

	l_1	l_2	\dots	$l_{ L }$
l_1				
l_2				
\vdots				
$l_{ L }$				

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

Landmark-Landmark Distances

	l_1	l_2	\dots	$l_{ L }$
l_1				
l_2				
\vdots				
$l_{ L }$				

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

Landmark-Landmark Distances

- Random access \Rightarrow fixed length encoding

	l_1	l_2	\dots	$l_{ L }$
l_1				
l_2				
\vdots				
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Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

$$v_1 \rightarrow [(l_{1_1}, 1), \dots, (l_{1_k}, 2)]$$

$$v_2 \rightarrow [(l_{2_1}, 1), \dots, (l_{2_k}, 2)]$$

⋮

$$v_n \rightarrow [(l_{n_1}, 1), \dots, (l_{n_k}, 2)]$$

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Landmark-Landmark Distances

- Random access \Rightarrow fixed length encoding

Single Row Compression

$$v_1 \rightarrow [(10, 1), (2, 2), (11, 3)]$$

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

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Landmark-Landmark Distances

- Random access \Rightarrow fixed length encoding

Single Row Compression

$$v_1 \rightarrow [(10, 1), (2, 2), (11, 3)] \quad - \text{sort by id}$$

$$v_1 \rightarrow [(2, 2), (10, 1), (11, 3)]$$

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

$$v_1 \rightarrow [(l_{1_1}, 1), \dots, (l_{1_k}, 2)]$$

$$v_2 \rightarrow [(l_{2_1}, 1), \dots, (l_{2_k}, 2)]$$

⋮

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Landmark-Landmark Distances

- Random access \Rightarrow fixed length encoding

Single Row Compression

$$v_1 \rightarrow [(10, 1), (2, 2), (11, 3)] \quad - \text{sort by id}$$

$$v_1 \rightarrow [(2, 2), (10, 1), (11, 3)] \quad - \text{store gaps}$$

$$v_1 \rightarrow [(2, 2), (+8, 1), (+1, 3)]$$

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

$$v_1 \rightarrow [(l_{1_1}, 1), \dots, (l_{1_k}, 2)]$$

$$v_2 \rightarrow [(l_{2_1}, 1), \dots, (l_{2_k}, 2)]$$

⋮

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$$v_1 \rightarrow [(2, 2), (+8, 1), (+1, 3)] \quad - \text{Rice coding}$$

Compressing Three-Hop Landmark Data

Three-Hop Distance Estimation in Social Graphs

$$v_1 \rightarrow [(l_{1_1}, 1), \dots, (l_{1_k}, 2)]$$

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⋮

$$v_n \rightarrow [(l_{n_1}, 1), \dots, (l_{n_k}, 2)]$$

Neighbor List Compression

- Similarly, encode vertex information as diff to neighbor
- Take care of changing local landmarks

- Evaluation on three Social Graphs

Experimental Evaluation

Three-Hop Distance Estimation in Social Graphs

- Evaluation on three Social Graphs
- Here: *loc-gowalla* 197k vertices, 950k edges, diameter 16

Experimental Evaluation

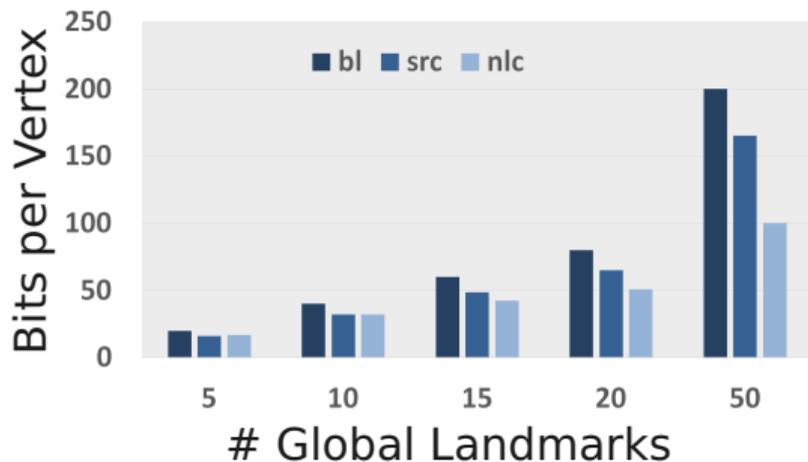
Three-Hop Distance Estimation in Social Graphs

- Evaluation on three Social Graphs
- Here: *loc-gowalla* 197k vertices, 950k edges, diameter 16
- Lots of parameters:
 - How to select landmarks globally and locally?
 - How many local / global landmarks?
 - Which queries are interesting?

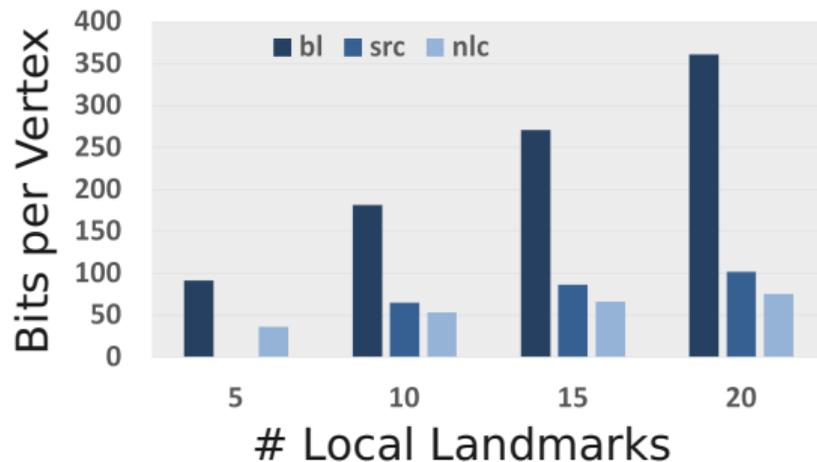
Compression Schemes

Three-Hop Distance Estimation in Social Graphs

Two-Hop



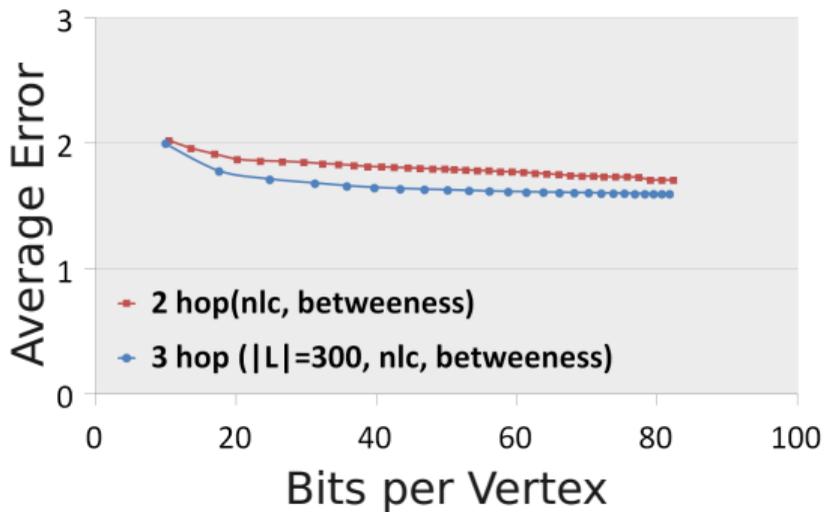
Three-Hop



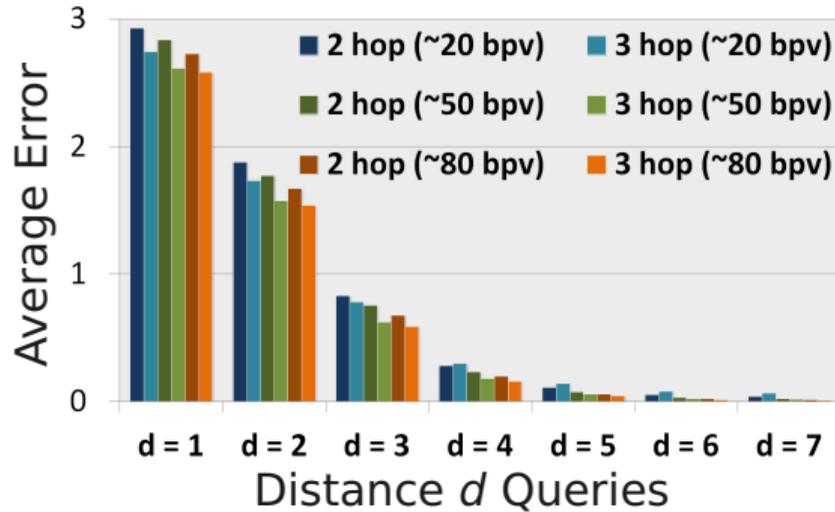
Space vs. Average Error

Three-Hop Distance Estimation in Social Graphs

Mixed Queries



Queries by Distance



Conclusion

Three-Hop Distance Estimation in Social Graphs

- Three-hop landmarks have an asymptotic advantage

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Three-Hop Distance Estimation in Social Graphs

- Three-hop landmarks have an asymptotic advantage
- They achieve a modest improvement over two-hop landmarks

Conclusion

Three-Hop Distance Estimation in Social Graphs

- Three-hop landmarks have an asymptotic advantage
- They achieve a modest improvement over two-hop landmarks
- *Sensible Compression makes a huge difference*